Transformers are Graph Neural Networks

Chaitanya K. Joshi

Graph Deep Learning Reading Group

Full Blogpost:

https://graphdeeplearning.github.io/post/transformers-are-gnns/

Some success stories: GNNs for RecSys



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Another success story? The Transformer architecture for NLP





Representation Learning for NLP



Breaking down the Transformer

We update the hidden feature h of the i'th word in a sentence S from layer ℓ to layer $\ell+1$ as follows:

$$egin{aligned} h_i^{\ell+1} &= ext{Attention}ig(Q^\ell h_i^\ell\,,K^\ell h_j^\ell\,,V^\ell h_j^\ellig), \ &i.\,e.\,,\ h_i^{\ell+1} &= \sum_{j\in\mathcal{S}} w_{ij}ig(V^\ell h_j^\ellig), \end{aligned}$$

 $ext{ where } w_{ij} = ext{softmax}_j ig(Q^\ell h_i^\ell \cdot K^\ell h_j^\ell ig),$

where $j \in S$ denotes the set of words in the sentence and Q, K, V are learnable linear weights.







Multi-head Attention

Bad random initializations can de-stabilize the learning process of this dot-product attention mechanism. We can 'hedge our bets' through concatenating multiple attention 'heads':

$$h_i^{\ell+1} = \text{Concat}(\text{head}_1, \dots, \text{head}_K) O^{\ell},$$
$$\text{ead}_k = \text{Attention}(O^{k,\ell} h^{\ell} - K^{k,\ell} h^{\ell} - V^{k,\ell} h^{\ell})$$

head_k = Attention $(Q^{\kappa,\epsilon}h_i^{\epsilon}, K^{\kappa,\epsilon}h_j^{\epsilon}, V^{\kappa,\epsilon}h_j^{\epsilon}),$



The Final Picture

Update each word's features through Multi-head Attention mechanism as a weighted sum of features of other words in the sentence.

+ Scaling dot product attention

+ Normalization layers

+ Residual links





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Representation Learning on Graphs



Graph Neural Networks

GNNs update the hidden features h of node i at layer ℓ via a non-linear transformation of the node's own features added to the aggregation of features from each neighbouring node $j \in N(i)$:

$$h_i^{\ell+1} = \sigma \Big(U^\ell h_i^\ell + \sum_{j \in \mathcal{N}(i)} (V^\ell h_j^\ell) \Big),$$

where U, V are learnable weight matrices of the GNN layer and σ is a non-linearity.



Connections b/w GNNs and Transformers



Consider a sentence as a fully connected graph of words...

Connections b/w GNNs and Transformers







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Transformer

